On the Galois module structure of integers of p-adic fields. The question of the minimal index

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Let L/K be a Galois extension with Galois group G. The Normal Basis Theorem shows that L is a free $K[G]$-module of rank 1. When L/K is a number field or a local field extension, it is natural to consider the question of determining the structure of the ring of integers $\mathcal{O}_L$ as a $\mathcal{O}_K[G]$-module. It is well-known that $\mathcal{O}_L$ contains free $\mathcal{O}_K[G]$-submodules of finite index, but, in general, it is not free.
In this talk, after a brief overview of the main classical results in this context, I will present some recent results on the minimal index of a free $\mathcal{O}_K[G]$-submodule into $\mathcal{O}_L$, in the case of p-adic fields.