Gauss-Lucas theorem in polynomial dynamics

Margaret Stawiska Friedland American Mathematical Society/MathSciNet stawiska@umich.edu

Using versions of the Gauss-Lucas theorem adapted to dynamics, we prove that for every complex polynomial p of degree $d \ge 2$ the convex hull H_p of the Julia set J_p of p satisfies $p^{-1}(H_p) \subset H_p$. This settles positively a conjecture by P. Alexandersson. We also characterize the families of polynomials for which the equality $p^{-1}(H_p) = H_p$ is achieved.