

## Connected $(n_k)$ configurations exist for almost all $n$

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A geometric  $(n_k)$  configuration is a collection of points and straight lines, typically in the Euclidean plane, so that each line passes through  $k$  of the points and each of the points lies on  $k$  of the lines. In a series of papers, Branko Grünbaum showed that geometric  $(n_4)$  configurations exist for all  $n \geq 24$ , using a series of geometric constructions later called the “Grünbaum Calculus”. In this talk, we will show that for each  $k > 4$ , there exists an integer  $N_k$  so that for *all*  $n \geq N_k$ , there exists at least one  $(n_k)$  configuration, by generalizing the Grünbaum Calculus operations to produce more highly incident configurations. This is joint work with Gábor Gévay and Tomaž Pisanski.